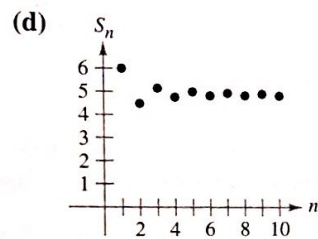
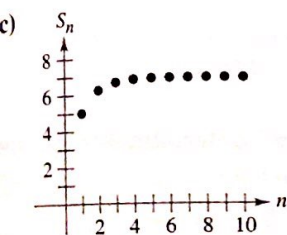
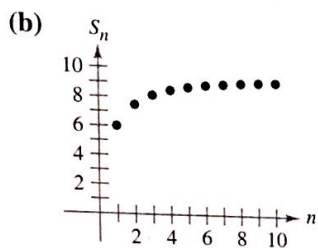
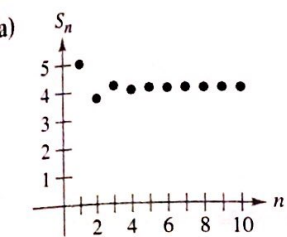


# EXERCISES FOR SECTION 8.5

In Exercises 1–4, match the series with the graph of its sequence of partial sums. [The graphs are labeled (a), (b), (c), and (d).]



1.  $\sum_{n=1}^{\infty} \frac{6}{n^2}$

2.  $\sum_{n=1}^{\infty} \frac{(-1)^{n-1} 6}{n^2}$

3.  $\sum_{n=1}^{\infty} \frac{10}{n2^n}$

4.  $\sum_{n=1}^{\infty} \frac{(-1)^{n-1} 10}{n2^n}$

**Numerical and Graphical Analysis** In Exercises 5–8, explore the Alternating Series Remainder.

(a) Use a graphing utility to find the indicated partial sum  $S_n$  and complete the table.

(b) Use a graphing utility to graph the first ten terms of the sequence of partial sums and a horizontal line representing the sum.

(c) What pattern exists between the plot of the successive points in part (b) relative to the horizontal line representing the sum of the series? Do the distances between the successive points and the horizontal line increase or decrease?

(d) Discuss the relationship between the answers in part (c) and the Alternating Series Remainder as given in Theorem 8.15.

$n$	1	2	3	4	5	6	7	8	9	10
$S_n$										

5.  $\sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{2n-1} = \frac{\pi}{4}$

6.  $\sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{(n-1)!} = \frac{1}{e}$

7.  $\sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{n^2} = \frac{\pi^2}{12}$

8.  $\sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{(2n-1)!} = \sin 1$

In Exercises 9–28, determine the convergence or divergence of the series.

✓ 9.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n}$

✓ 11.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{2n-1}$

✓ 13.  $\sum_{n=1}^{\infty} \frac{(-1)^n n^2}{n^2+1}$

✓ 15.  $\sum_{n=1}^{\infty} \frac{(-1)^n}{\sqrt{n}}$

✓ 17.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} (n+1)}{\ln(n+1)}$

19.  $\sum_{n=1}^{\infty} \sin \frac{(2n-1)\pi}{2}$

21.  $\sum_{n=1}^{\infty} \cos n\pi$

23.  $\sum_{n=0}^{\infty} \frac{(-1)^n}{n!}$

25.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} \sqrt{n}}{n+2}$

27.  $\sum_{n=1}^{\infty} \frac{2(-1)^{n+1}}{e^n - e^{-n}} = \sum_{n=1}^{\infty} (-1)^{n+1} \operatorname{csch} n$

28.  $\sum_{n=1}^{\infty} \frac{2(-1)^{n+1}}{e^n + e^{-n}} = \sum_{n=1}^{\infty} (-1)^{n+1} \operatorname{sech} n$

10.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} n}{2n-1}$  ✓

12.  $\sum_{n=1}^{\infty} \frac{(-1)^n}{\ln(n+1)}$  ✓

14.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} n}{n^2+1}$  ✓

16.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} n^2}{n^2+5}$  ✓

18.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} \ln(n+1)}{n+1}$  ✓

20.  $\sum_{n=1}^{\infty} \frac{1}{n} \sin \frac{(2n-1)\pi}{2}$  ✓

22.  $\sum_{n=1}^{\infty} \frac{1}{n} \cos n\pi$  ✓

24.  $\sum_{n=0}^{\infty} \frac{(-1)^n}{(2n+1)!}$  ✓

26.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} \sqrt{n}}{\sqrt[3]{n}}$  ✓

In Exercises 29–32, approximate the sum of the series by using the first six terms. (See Example 4.)

29.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} 3}{n^2}$

30.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} 4}{\ln(n+1)}$  ✓

31.  $\sum_{n=0}^{\infty} \frac{(-1)^n 2}{n!}$

32.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} n}{2^n}$  ✓

✎ In Exercises 33–38, (a) use Theorem 8.15 to determine the number of terms required to approximate the sum of the convergent series with an error of less than 0.001, and (b) use a graphing utility to approximate the sum of the series with an error of less than 0.001.

33.  $\sum_{n=0}^{\infty} \frac{(-1)^n}{n!} = \frac{1}{e}$

34.  $\sum_{n=0}^{\infty} \frac{(-1)^n}{2^n n!} = \frac{1}{\sqrt{e}}$

35.  $\sum_{n=0}^{\infty} \frac{(-1)^n}{(2n+1)!} = \sin 1$

36.  $\sum_{n=0}^{\infty} \frac{(-1)^n}{(2n)!} = \cos 1$

37.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} = \ln 2$

38.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n4^n} = \ln \frac{5}{4}$