

Before you begin the exercise set, be sure you realize that one of the most important steps in integration is *rewriting the integrand* in a form that fits the basic integration rules. To illustrate this point further, here are some additional examples.

| <u>Original Integral</u> | <u>Rewrite</u> | <u>Integrate</u> | <u>Simplify</u> |
|-------------------------------|--------------------------------|--|---|
| $\int \frac{2}{\sqrt{x}} dx$ | $2 \int x^{-1/2} dx$ | $2 \left(\frac{x^{1/2}}{1/2} \right) + C$ | $4x^{1/2} + C$ |
| $\int (t^2 + 1)^2 dt$ | $\int (t^4 + 2t^2 + 1) dt$ | $\frac{t^5}{5} + 2 \left(\frac{t^3}{3} \right) + t + C$ | $\frac{1}{5}t^5 + \frac{2}{3}t^3 + t + C$ |
| $\int \frac{x^3 + 3}{x^2} dx$ | $\int (x + 3x^{-2}) dx$ | $\frac{x^2}{2} + 3 \left(\frac{x^{-1}}{-1} \right) + C$ | $\frac{1}{2}x^2 - \frac{3}{x} + C$ |
| $\int \sqrt[3]{x}(x - 4) dx$ | $\int (x^{4/3} - 4x^{1/3}) dx$ | $\frac{x^{7/3}}{7/3} - 4 \left(\frac{x^{4/3}}{4/3} \right) + C$ | $\frac{3}{7}x^{7/3} - 3x^{4/3}$ |

Exercises for Section 4.1

See www.CalcChat.com for worked-out solutions to odd-numbered exercises.

In Exercises 1–4, verify the statement by showing that the derivative of the right side equals the integrand of the left side.

- $\int \left(-\frac{9}{x^4} \right) dx = \frac{3}{x^3} + C$
- $\int \left(4x^3 - \frac{1}{x^2} \right) dx = x^4 + \frac{1}{x} + C$
- $\int (x - 2)(x + 2) dx = \frac{1}{3}x^3 - 4x + C$
- $\int \frac{x^2 - 1}{x^{3/2}} dx = \frac{2(x^2 + 3)}{3\sqrt{x}} + C$

In Exercises 5–8, find the general solution of the differential equation and check the result by differentiation.

- $\frac{dy}{dt} = 3t^2$
- $\frac{dr}{d\theta} = \pi$
- $\frac{dy}{dx} = x^{3/2}$
- $\frac{dy}{dx} = 2x^{-3}$

In Exercises 9–14, complete the table.

| <u>Original Integral</u> | <u>Rewrite</u> | <u>Integrate</u> | <u>Simplify</u> |
|-----------------------------------|----------------|------------------|-----------------|
| 9. $\int \sqrt[3]{x} dx$ | | | |
| 10. $\int \frac{1}{x^2} dx$ | | | |
| 11. $\int \frac{1}{x\sqrt{x}} dx$ | | | |
| 12. $\int x(x^2 + 3) dx$ | | | |
| 13. $\int \frac{1}{2x^3} dx$ | | | |
| 14. $\int \frac{1}{(3x)^2} dx$ | | | |

In Exercises 15–34, find the indefinite integral and check the result by differentiation.

- $\int (x + 3) dx$
- $\int (5 - x) dx$
- $\int (2x - 3x^2) dx$
- $\int (4x^3 + 6x^2 - 1) dx$
- $\int (x^3 + 2) dx$
- $\int (x^3 - 4x + 2) dx$
- $\int (x^{3/2} + 2x + 1) dx$
- $\int \left(\sqrt{x} + \frac{1}{2\sqrt{x}} \right) dx$
- $\int \sqrt[3]{x^2} dx$
- $\int (\sqrt[4]{x^3} + 1) dx$
- $\int \frac{1}{x^3} dx$
- $\int \frac{1}{x^4} dx$
- $\int \frac{x^2 + x - 3}{x^4} dx$
- $\int (x^2 + x + 1) dx$
- $\int \frac{x^2 + 2x - 3}{x^4} dx$
- $\int (x + 1)(3x - 2) dx$
- $\int (2t^2 - 1)^2 dt$
- $\int y^2 \sqrt{y} dy$
- $\int (1 + 3t)t^2 dt$
- $\int dx$
- $\int 3 dt$

In Exercises 35–42, find the indefinite integral and check the result by differentiation.

- $\int (2 \sin x + 3 \cos x) dx$
- $\int (t^2 - \sin t) dt$
- $\int (1 - \csc t \cot t) dt$
- $\int (\theta^2 + \sec^2 \theta) d\theta$
- $\int (\sec^2 \theta - \sin \theta) d\theta$
- $\int \sec y (\tan y - \sec y) dy$
- $\int (\tan^2 y + 1) dy$
- $\int \frac{\cos x}{1 - \cos^2 x} dx$