

## THEOREM 1.2 Properties of Limits

Let  $b$  and  $c$  be real numbers, let  $n$  be a positive integer, and let  $f$  and  $g$  be functions with the limits

$$\lim_{x \rightarrow c} f(x) = L \quad \text{and} \quad \lim_{x \rightarrow c} g(x) = K.$$

1. Scalar multiple:  $\lim_{x \rightarrow c} [b f(x)] = bL$
2. Sum or difference:  $\lim_{x \rightarrow c} [f(x) \pm g(x)] = L \pm K$
3. Product:  $\lim_{x \rightarrow c} [f(x)g(x)] = LK$
4. Quotient:  $\lim_{x \rightarrow c} \frac{f(x)}{g(x)} = \frac{L}{K}, \quad K \neq 0$
5. Power:  $\lim_{x \rightarrow c} [f(x)]^n = L^n$

A proof of this theorem is given in Appendix A.

See [LarsonCalculus.com](http://LarsonCalculus.com) for Bruce Edwards's video of this proof.

### **THEOREM 1.5 The Limit of a Composite Function**

If  $f$  and  $g$  are functions such that  $\lim_{x \rightarrow c} g(x) = L$  and  $\lim_{x \rightarrow L} f(x) = f(L)$ , then

$$\lim_{x \rightarrow c} f(g(x)) = f\left(\lim_{x \rightarrow c} g(x)\right) = f(L).$$

A proof of this theorem is given in Appendix A.

See [LarsonCalculus.com](http://LarsonCalculus.com) for Bruce Edwards's video of this proof.